

# **Drawing in 3D**

**CSCI 4229/5229**  
**Computer Graphics**  
**Fall 2006**

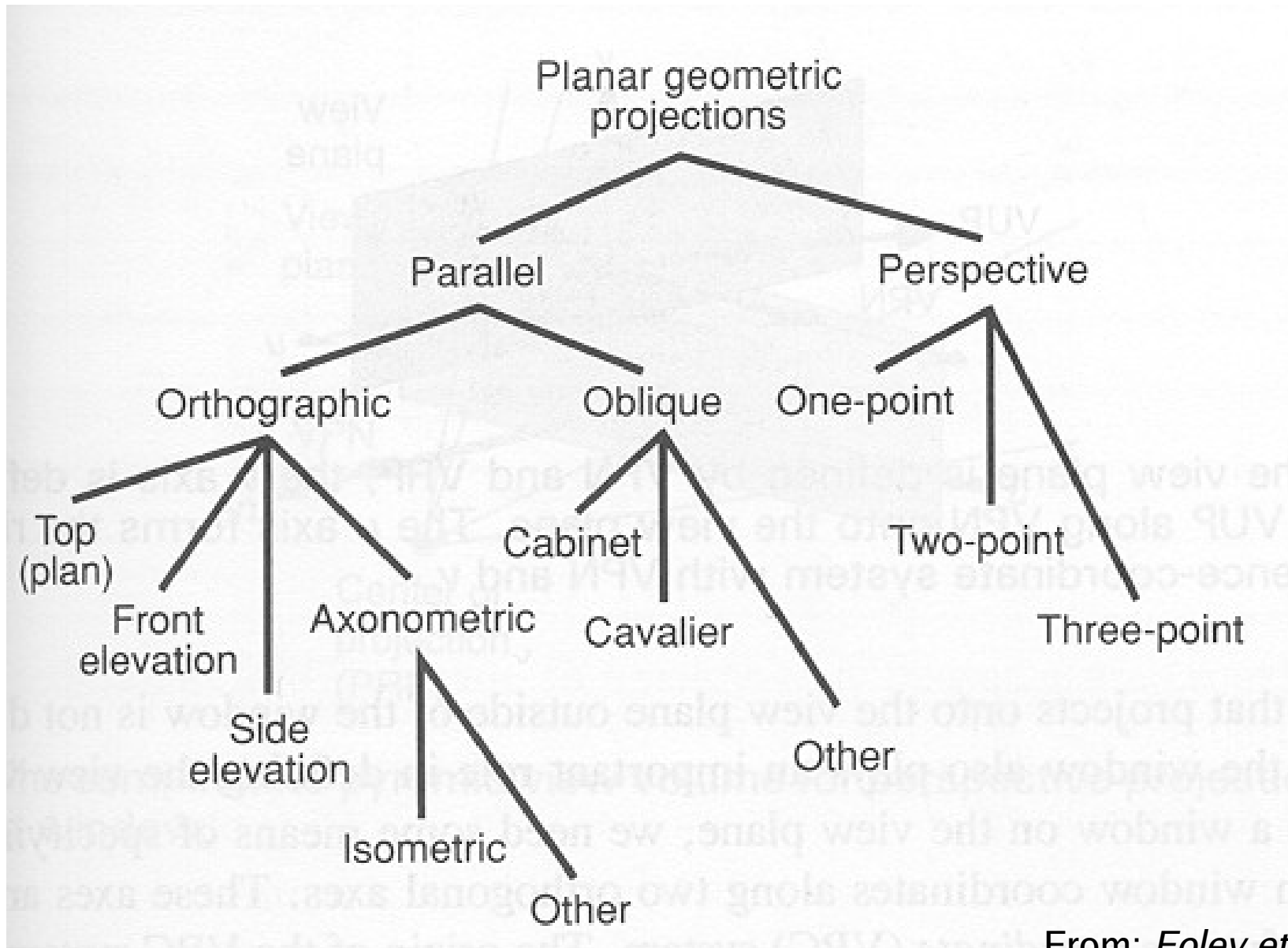
# Differences from 2D

- The third dimension (duh!)
- Depth perception
- Hidden lines and surfaces
- Realism
  - Lighting
  - Shading
  - Texture

# Types of Projections

- Parallel Projections
  - Orthogonal, isometric, ...
  - Size does not diminish with distance
- Perspective
  - Realistic based on an observer's point of view
  - Nearer bigger, further smaller
  - One or more vanishing points

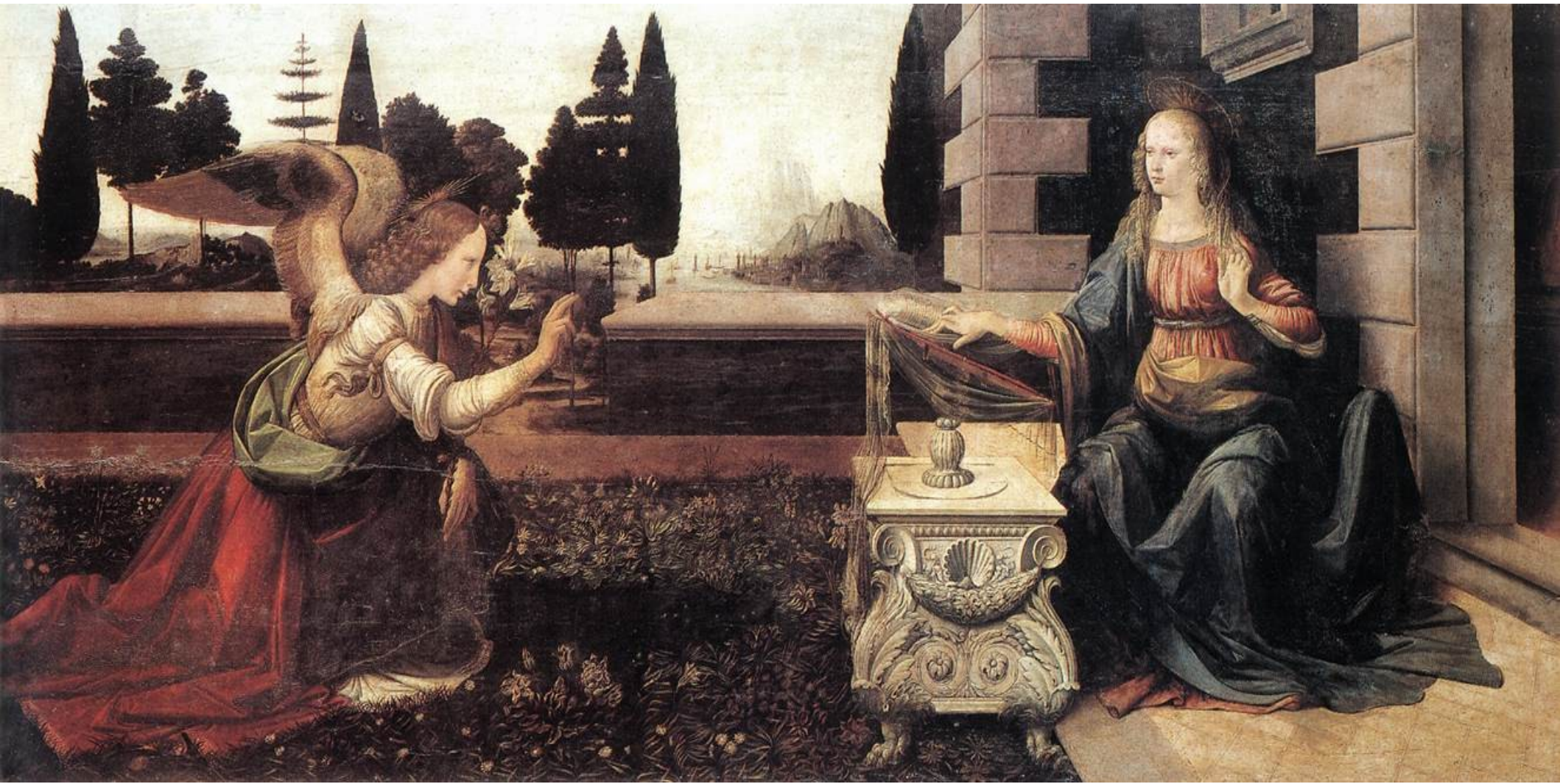
# Taxonomy of Projections



From: *Foley et al*

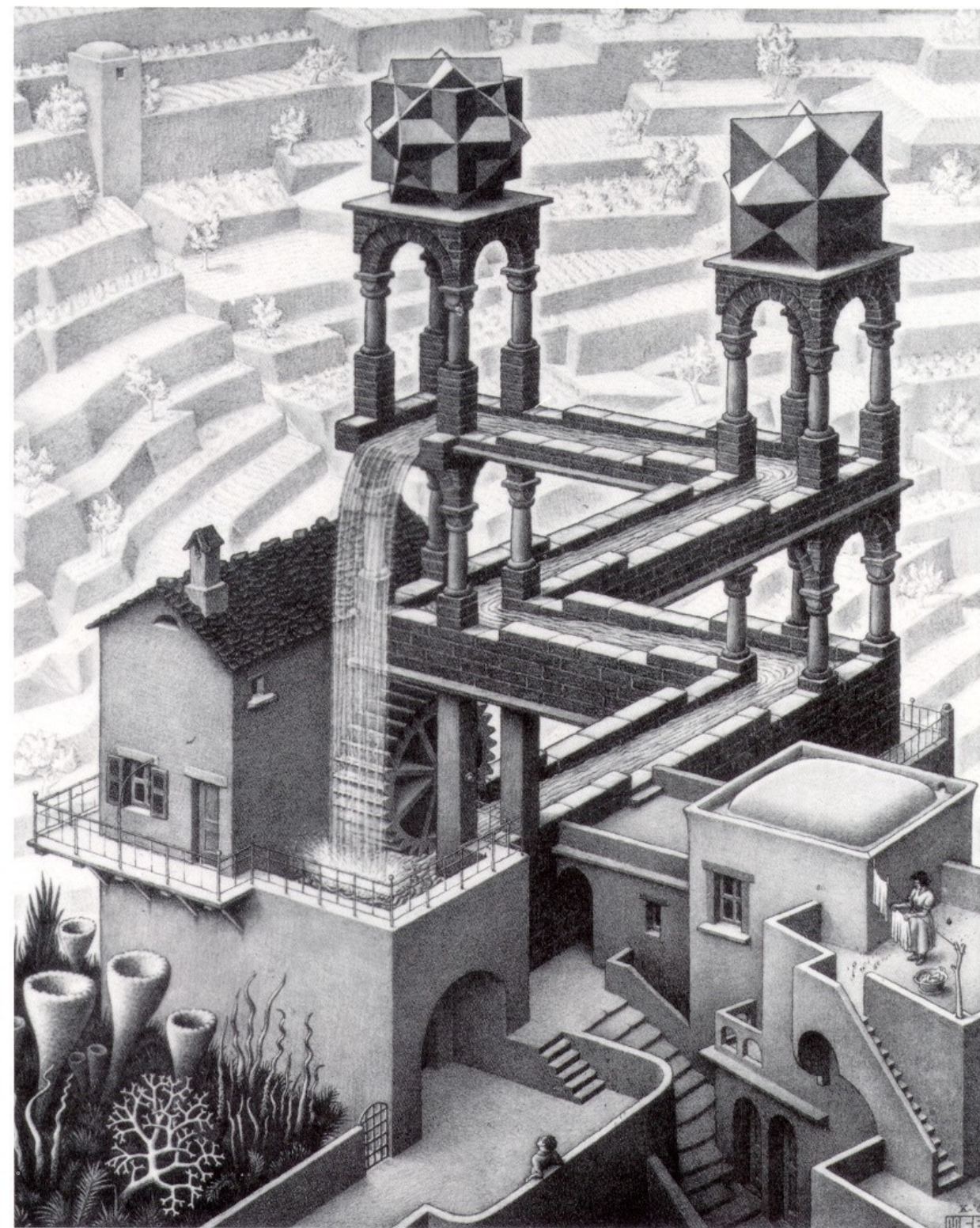
# *Annunciation*

## Leonardo da Vinci (1472)

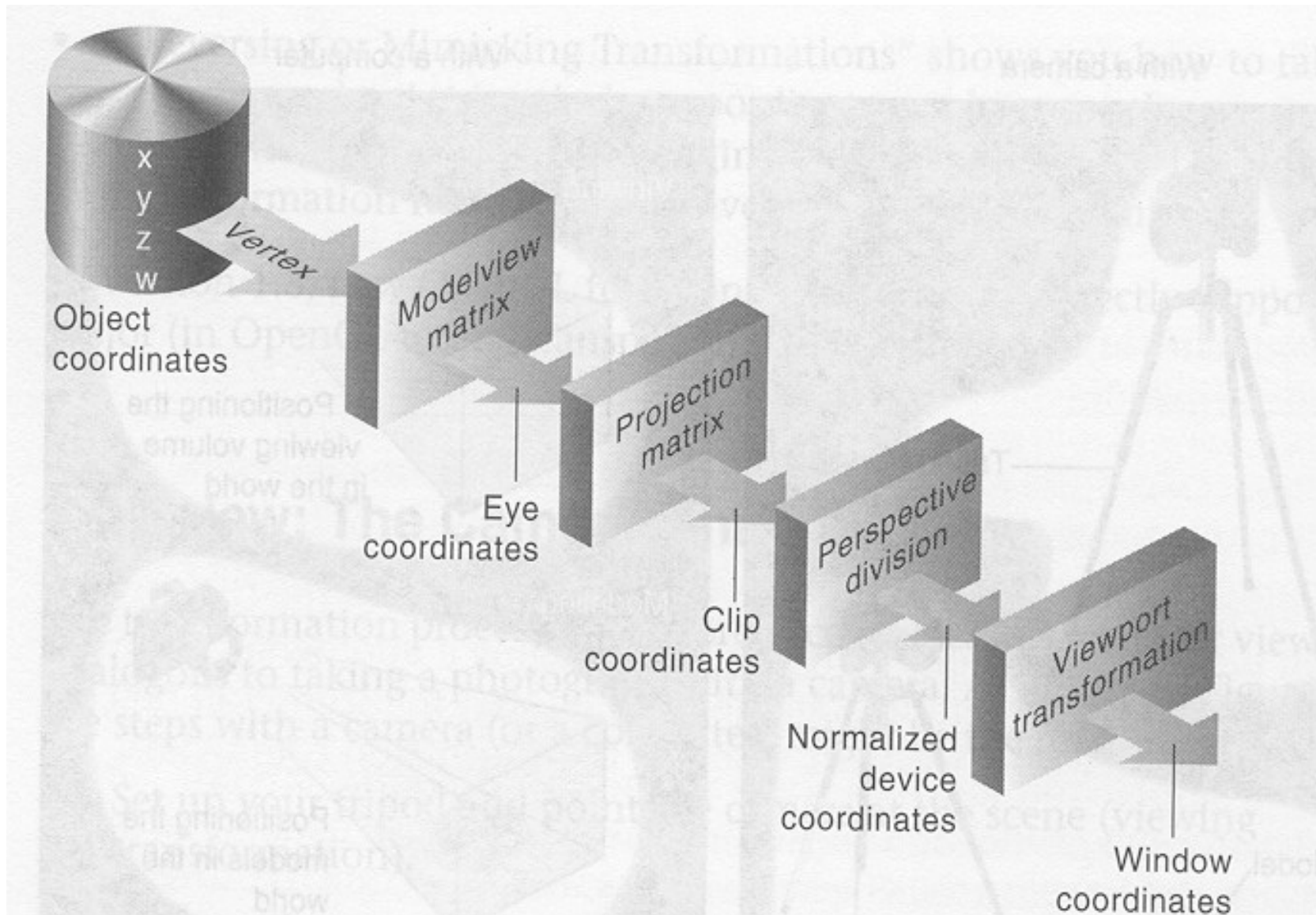


# Waterfall

M.C. Escher (1961)

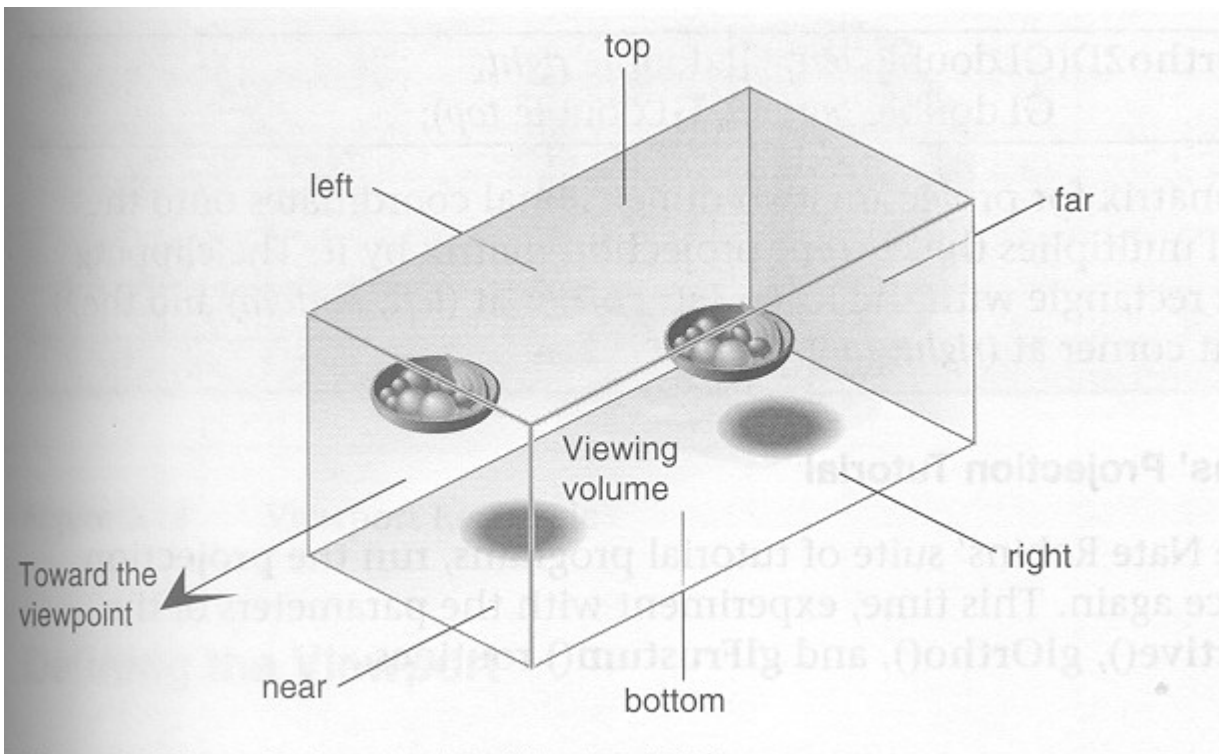


# OpenGL Transformation Pipeline



# Parallel Projection

- Apply rotation matrix to map direction of projection to  $Z$  axis and up to  $Y$  axis
- Scale to canonical volume



From: *OpenGL  
Red Book*



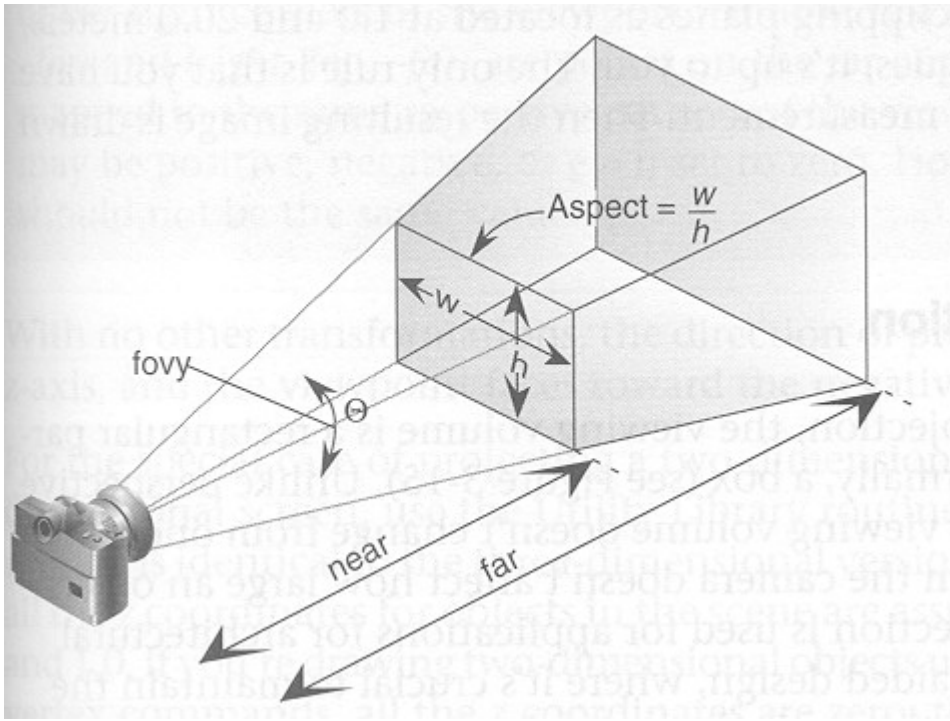
**glOrtho( $x_{min}, x_{max}, y_{min}, y_{max}, z_{min}, z_{max}$ )**

glOrtho Projection Matrix

$$\begin{pmatrix} \frac{2}{x_{max} - x_{min}} & 0 & 0 & \frac{x_{max} + x_{min}}{x_{max} - x_{min}} \\ 0 & \frac{2}{y_{max} - y_{min}} & 0 & \frac{y_{max} + y_{min}}{y_{max} - y_{min}} \\ 0 & 0 & \frac{2}{z_{max} - z_{min}} & \frac{z_{max} + z_{min}}{z_{max} - z_{min}} \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

# Perspective Transformation

- Apply rotation matrix to map eye position to center of scene to negative  $Z$  and up to  $Y$  axes
- Scale  $(x,y)$  inversely proportional to distance
- Scale to canonical volume



From: *OpenGL  
Red Book*

# gluPerspective(fovy, aspect, Znear, Zfar)

Let  $\theta = \text{fovy}/2$

gluPerspective Projection Matrix

$$\begin{pmatrix} \frac{\cot \theta}{\text{aspect}} & 0 & 0 & 0 \\ 0 & \cot \theta & 0 & 0 \\ 0 & 0 & \frac{z_{\text{far}} + z_{\text{near}}}{z_{\text{far}} - z_{\text{near}}} & \frac{2z_{\text{far}}z_{\text{near}}}{z_{\text{far}} - z_{\text{near}}} \\ 0 & 0 & -1 & 0 \end{pmatrix}$$

# `gluPerspective(fovy, aspect, Znear, Zfar)`

- *fovy* is the angle in the up/down direction
- *aspect* is the horizontal to vertical ratio
- *Znear* is the distance to the near clipping plane
  - Killer fact  $Znear > 0$
- *Zfar* is the distance to the far clipping plane
  - $Zfar > Znear$
- *Zfar-Znear* determines *Z* resolution since the *Z* buffer has finite precision

$\text{gluLookAt}(E_x, E_y, E_z, C_x, C_y, C_z, U_x, U_y, U_z)$

- $(E_x, E_y, E_z)$  is the eye position
- $(C_x, C_y, C_z)$  is the position you look at
- $(U_x, U_y, U_z)$  is the up direction
- $C-E$  determines the distance in the  $Z$  direction
- The  $Z$  distance to each object (from  $E$ ) determines the reduction in the  $(x, y)$  direction