# Ray Tracing: Mandelbulb

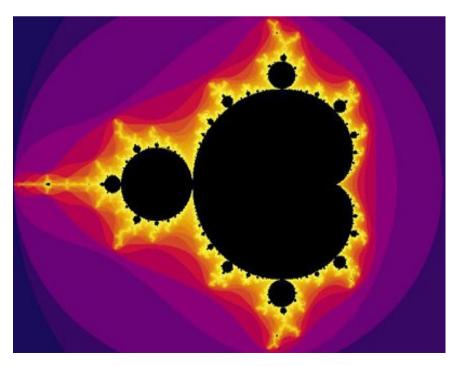
CSCI 4830/7000
Advanced Computer Graphics
Spring 2012

#### Mandelbrot Set

Complex Quadratic Polynomial Sequence

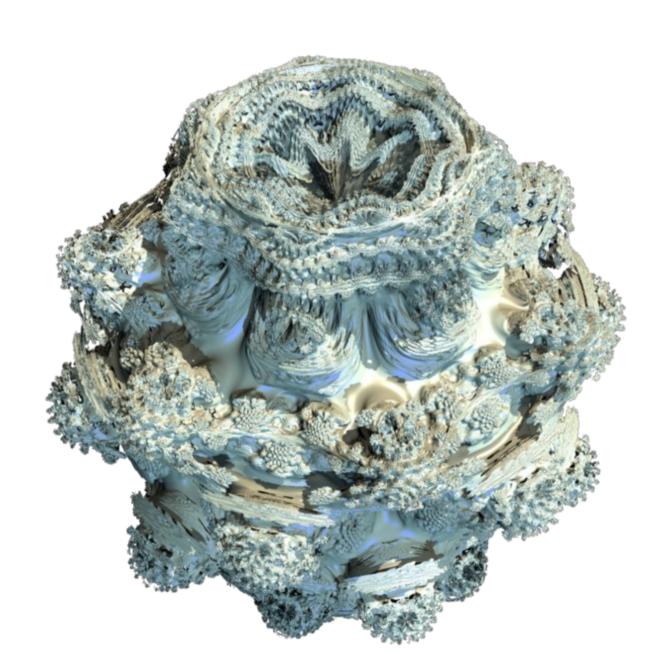
$$-Z_{n+1} = Z_n^2 + C$$

- For which values of c is the sequence bounded?
- This is a fractal set
  - Finite area
  - Boundary is infinite
  - Self-similar
  - 2D



#### Mandlebulb 3D Domain

- Defined mathematically
- Has appearance of Gothic architecure
- Shading needed to see details



## Mandelbulb Equation

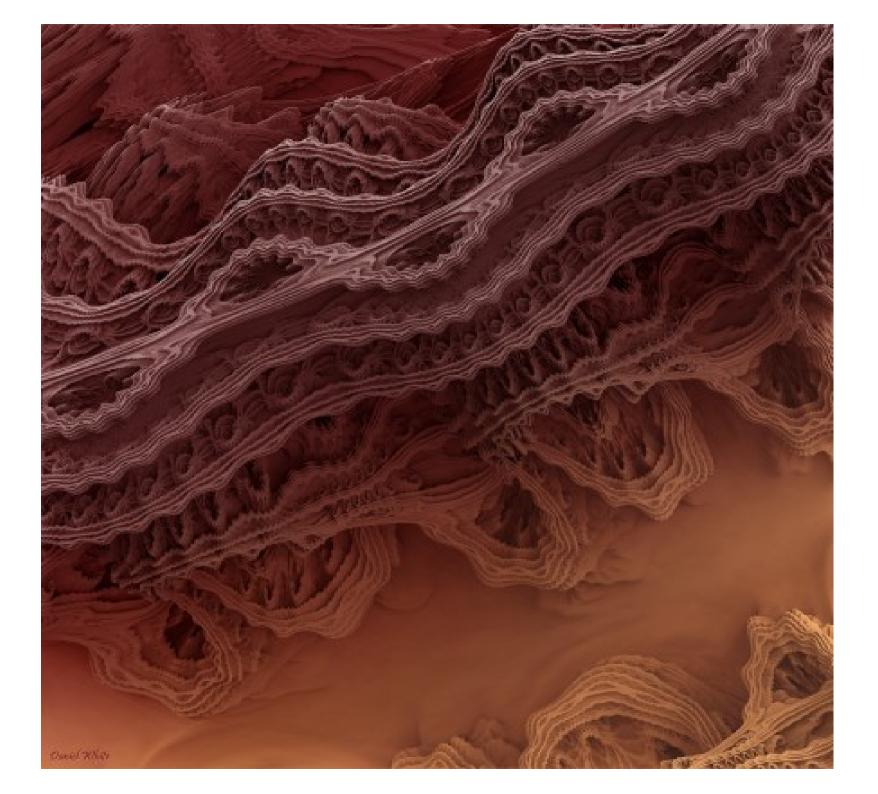
• 
$$Z_{n+1} = Z_n^2 + C$$

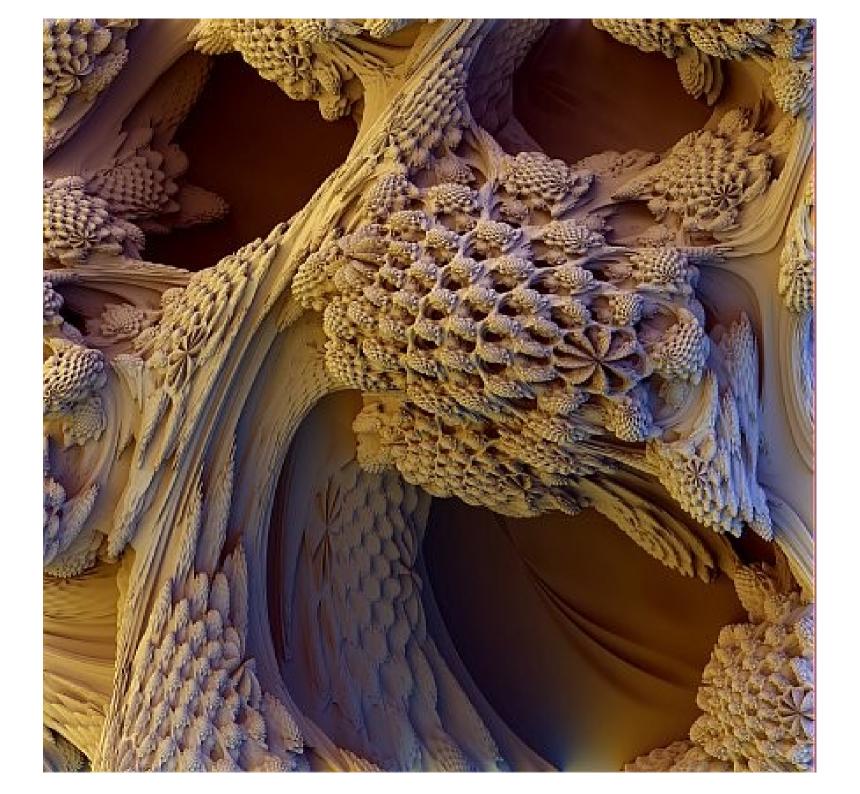
- Domain for this equation converges
- No direct equivalent to complex for 2D
- White and Nylander spherical coordinates
- How do you render this set?
  - POVray used for many images
  - ex25 and ex26 are primitive but real time
- See handout for details

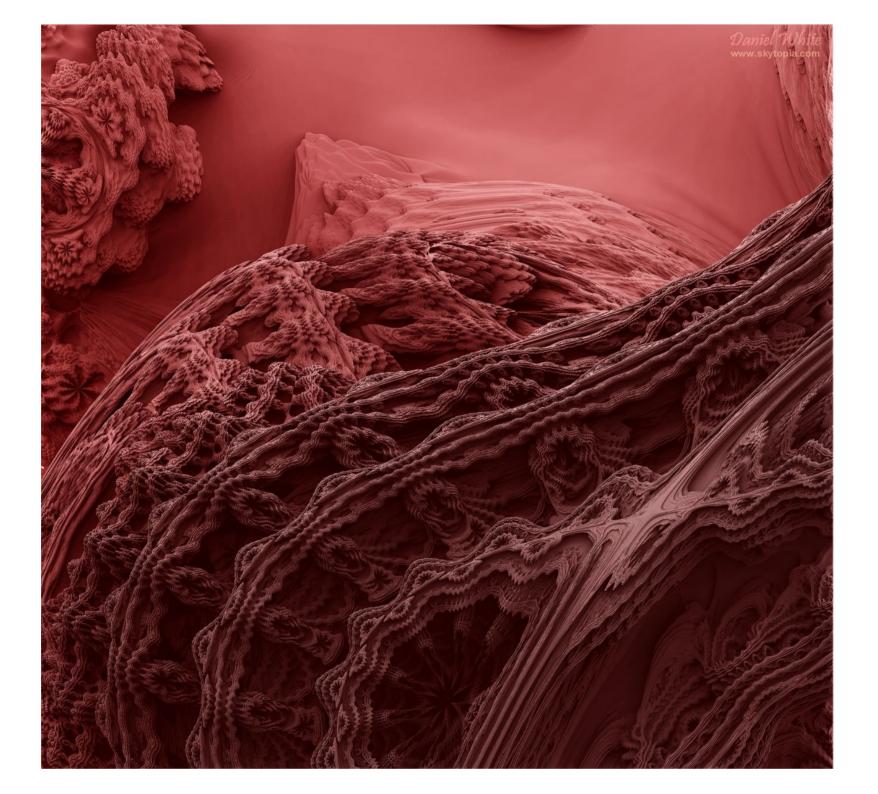
### Gallery of Daniel White

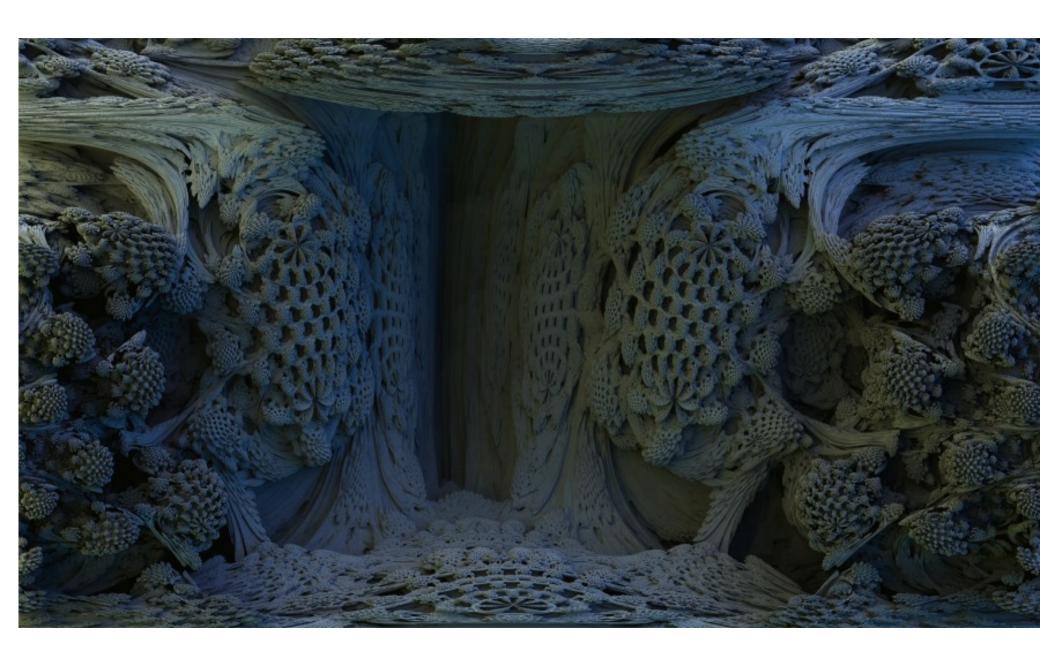
- The Unravelling the Real 3D Mandelbulb http://www.skytopia.com/project/fractal/mandelbulb.html
- Explores and zooms into the mandelbulb
- Ray traced using colored lights
- Most are the n=8 mandelbulb

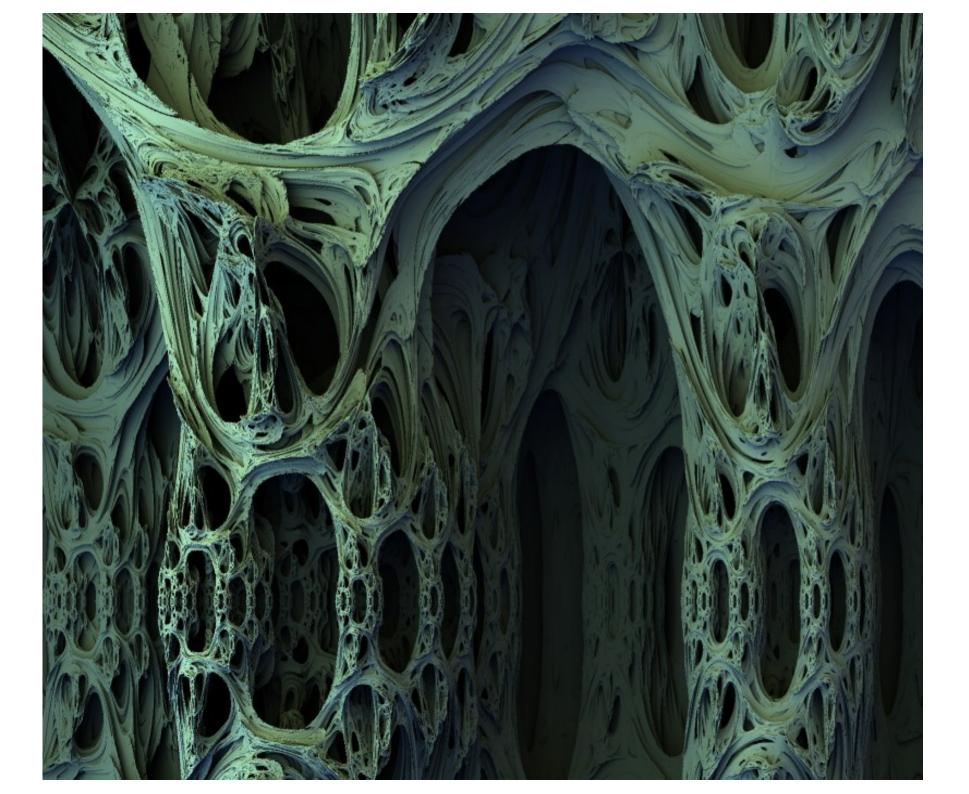


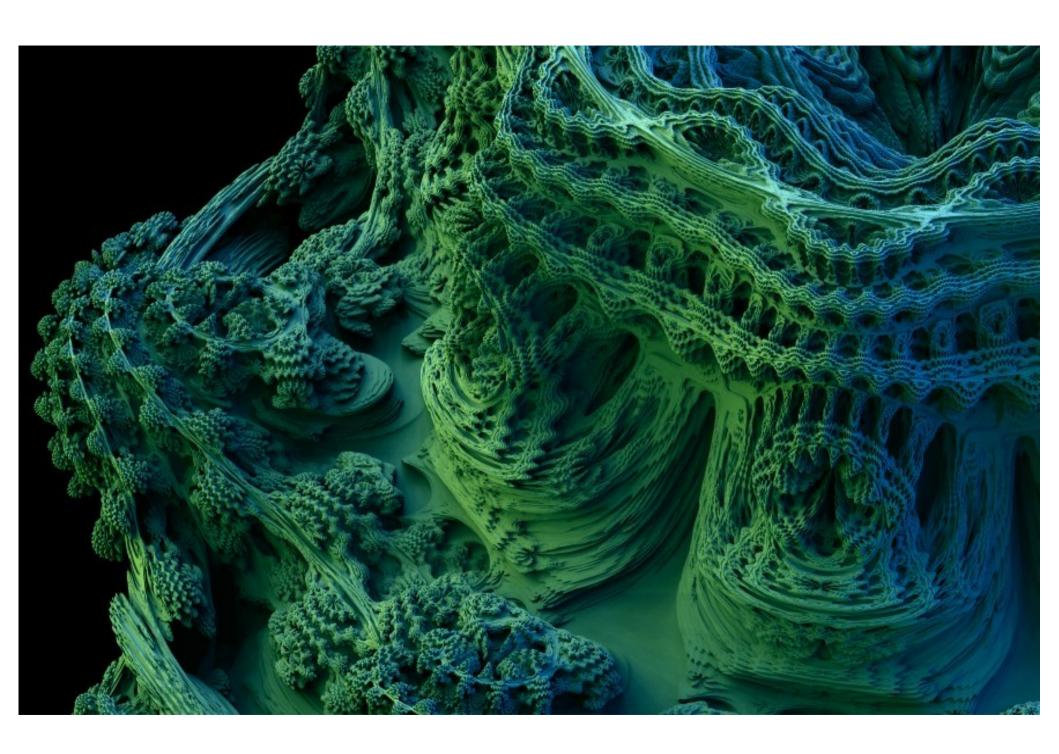






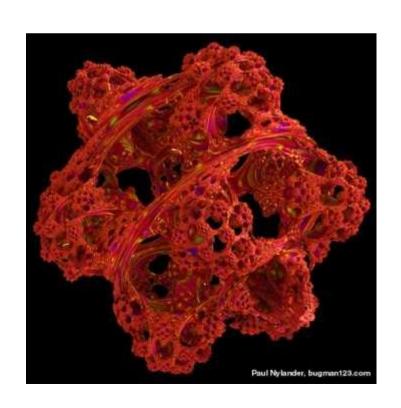






#### Other Fractal Sets

- Mandelbrot set is just one of many 2D fractal sets
  - Julia
  - Lyapunov
  - Sierpinski triangle
- Many extensions to 3D



## Real Time Ray Tracer

- ex25
  - Iterative solver for ray marching
  - OpenMP for parallel rays
- ex26
  - Adapts ex25 to CUDA
- Why not use GLSL?