# Ray Tracing: Mandelbulb

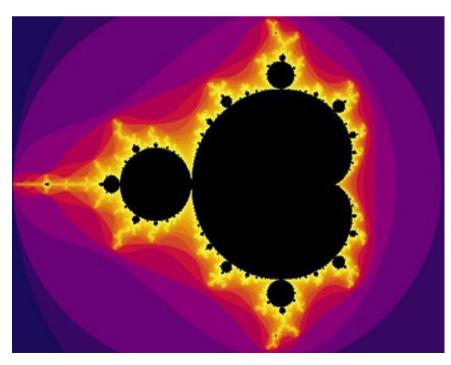
CSCI 4239/5239
Advanced Computer Graphics
Spring 2015

#### Mandelbrot Set

Complex Quadratic Polynomial Sequence

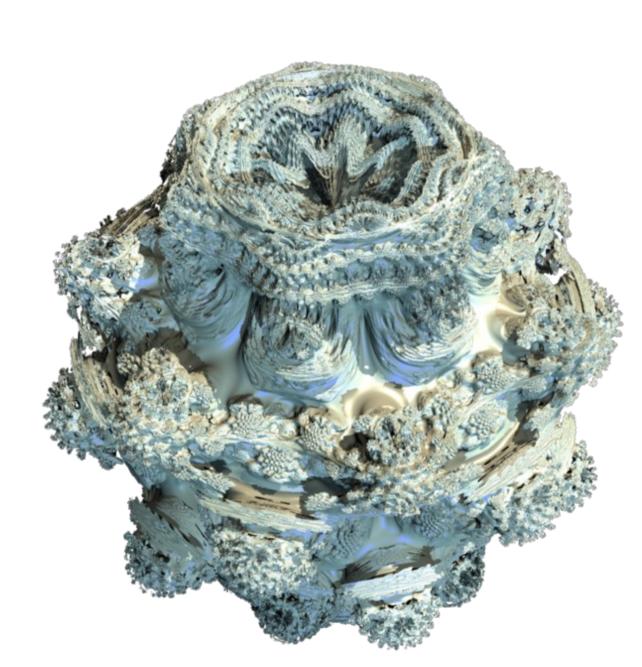
$$-Z_{n+1} = Z_n^2 + C$$

- For which values of c is the sequence bounded?
- This is a fractal set
  - Finite area
  - Boundary is infinite
  - Self-similar
  - 2D



#### Mandlebulb 3D Domain

- Defined mathematically
- Has appearance of Gothic architecure
- Shading needed to see details



## Mandelbulb Equation

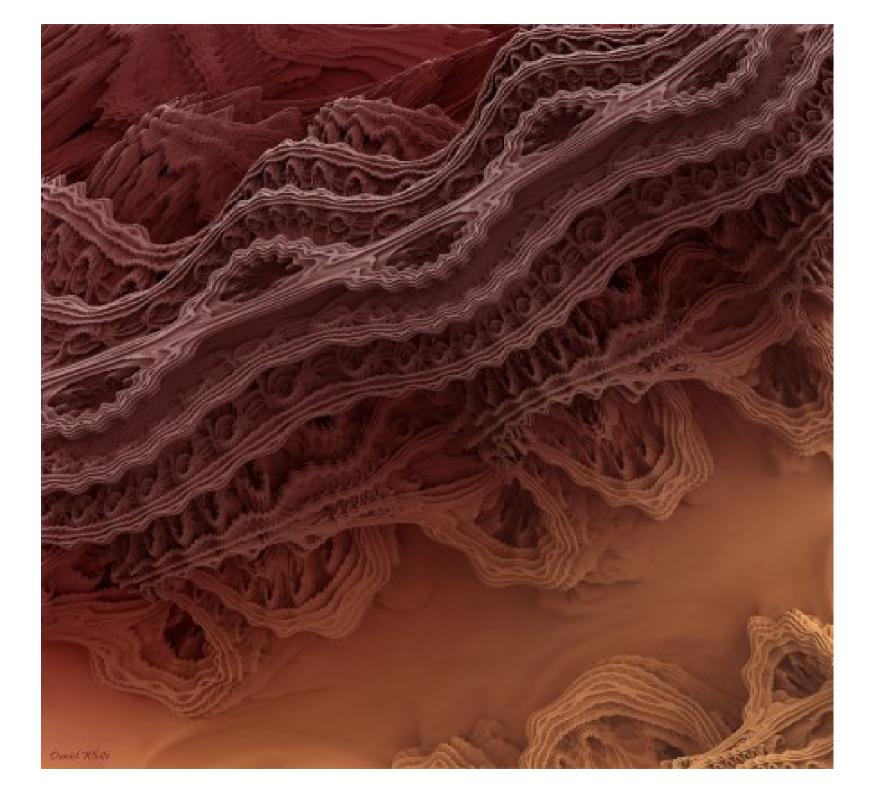
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$$Z_{n+1} = Z_n^2 + C$$

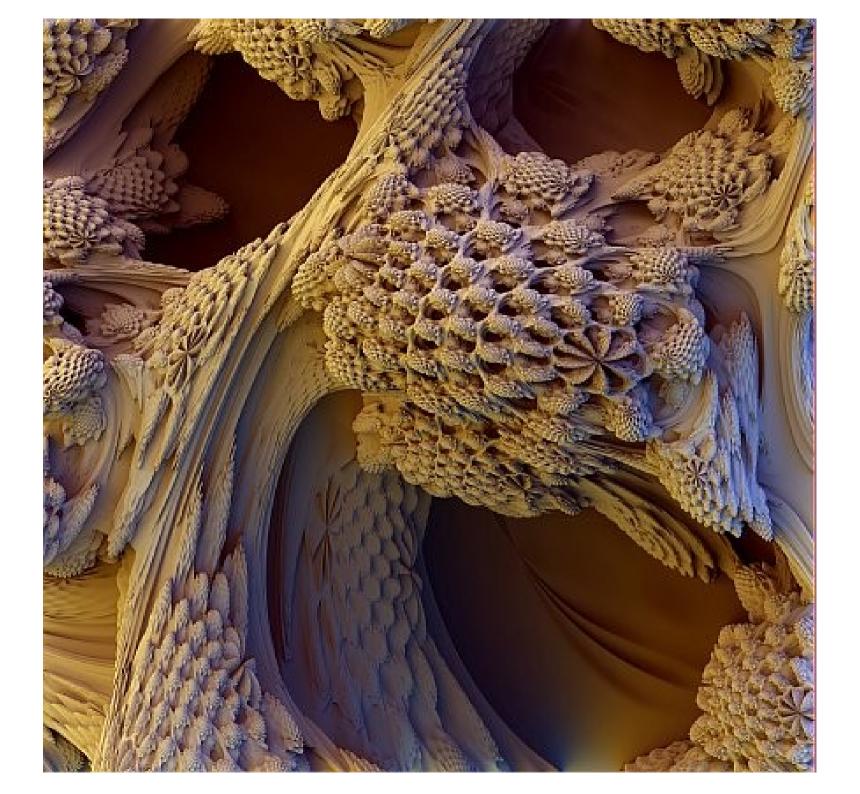
- Domain for this equation converges
- No direct equivalent to complex for 2D
- White and Nylander spherical coordinates
- How do you render this set?
  - POVray used for many images
  - ex28 is primitive but real time
- See handout for details

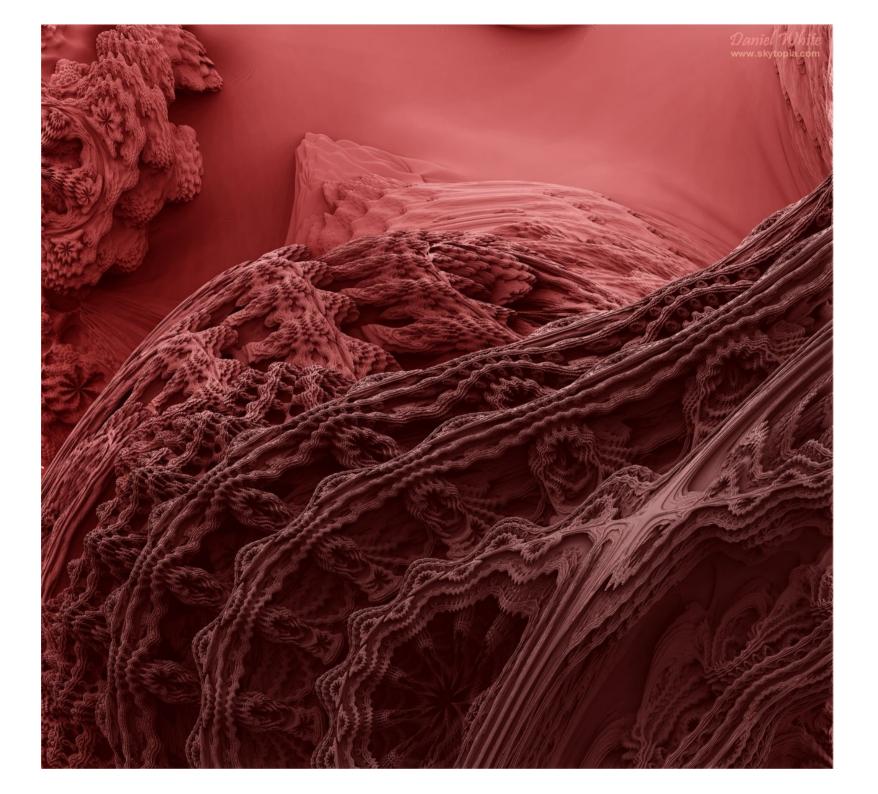
## Gallery of Daniel White

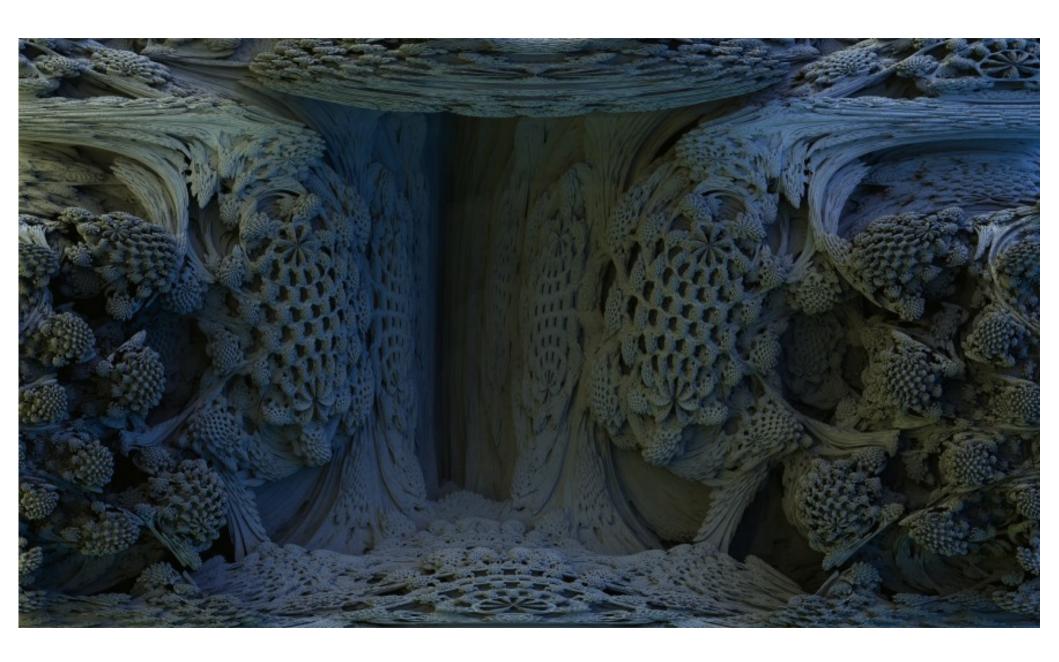
- The Unravelling the Real 3D Mandelbulb http://www.skytopia.com/project/fractal/mandelbulb.html
- Explores and zooms into the mandelbulb
- Ray traced using colored lights
- Most are the n=8 mandelbulb

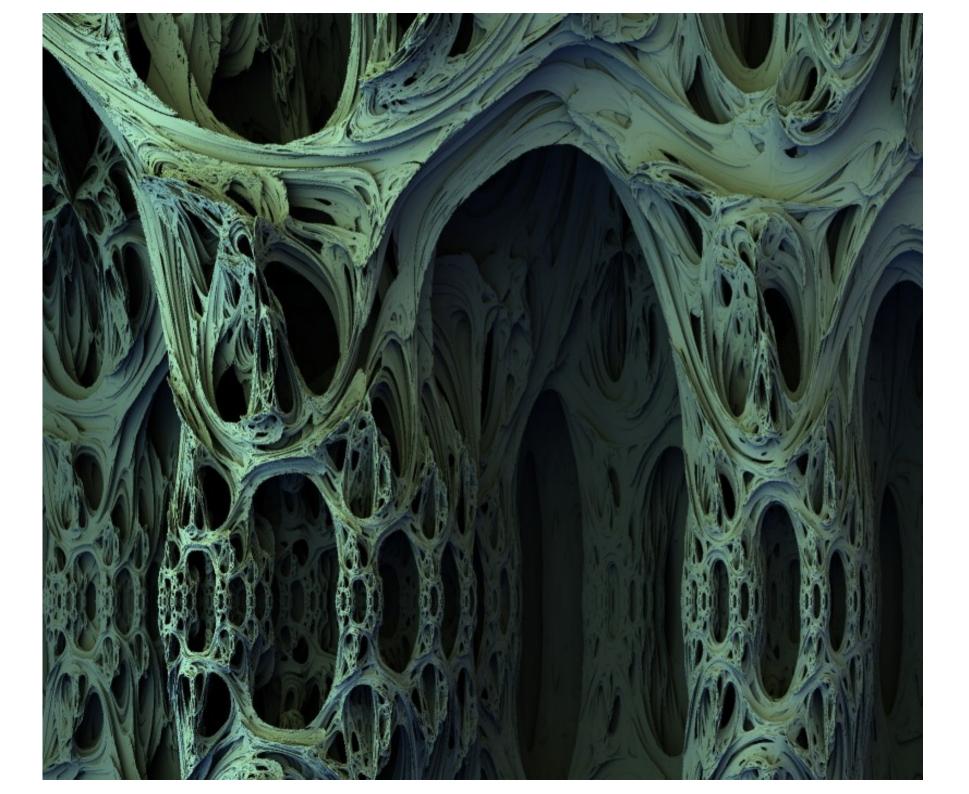


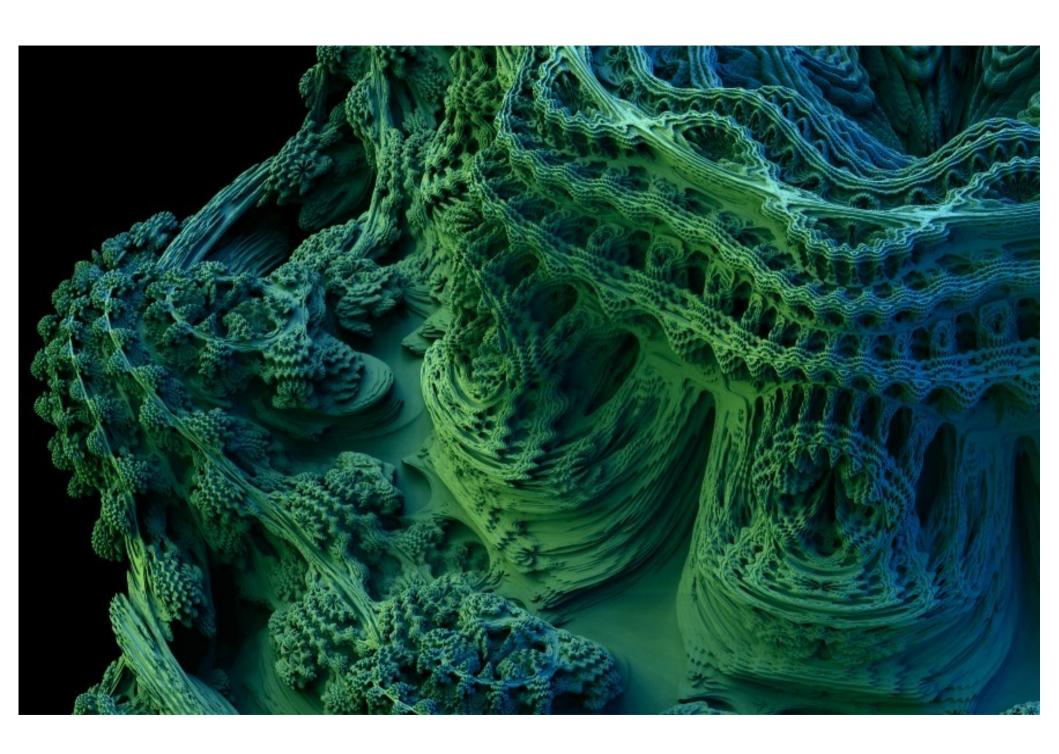






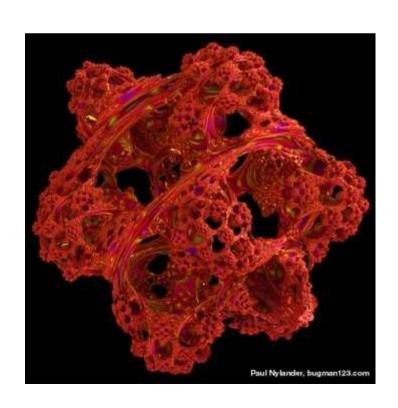






#### Other Fractal Sets

- Mandelbrot set is just one of many 2D fractal sets
  - Julia
  - Lyapunov
  - Sierpinski triangle
- Many extensions to 3D



### ex28: Real Time Ray Tracer

- Draws monochrome mandelbulb
  - Single light
  - No secondary rays
  - Shadows
- Iterative solver for ray marching
  - OpenMP on CPU
  - CUDA on GPU
- Why not use GLSL?
  - Perhaps a compute shader?