Ray Tracing: Mandelbulb

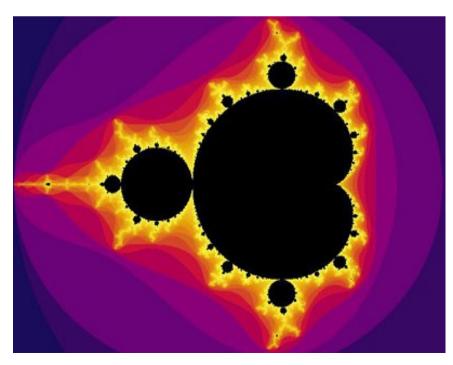
CSCI 4239/5239
Advanced Computer Graphics
Spring 2013

Mandelbrot Set

Complex Quadratic Polynomial Sequence

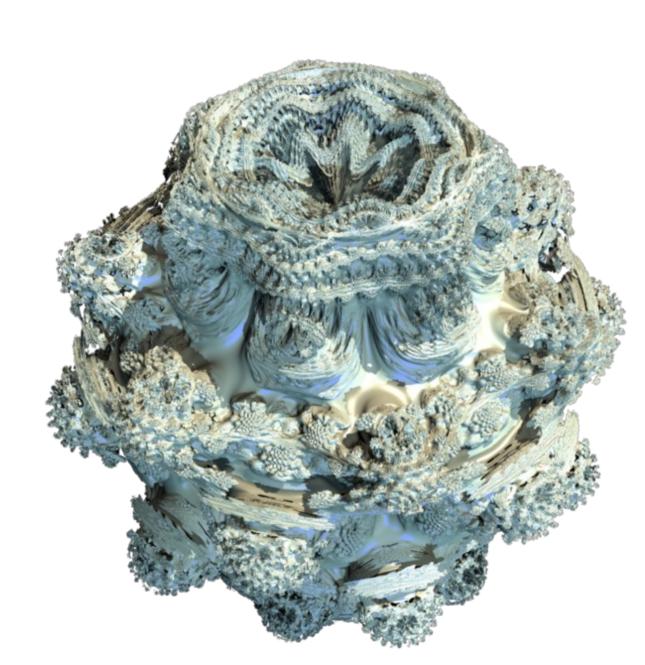
$$-Z_{n+1} = Z_n^2 + C$$

- For which values of c is the sequence bounded?
- This is a fractal set
 - Finite area
 - Boundary is infinite
 - Self-similar
 - 2D



Mandlebulb 3D Domain

- Defined mathematically
- Has appearance of Gothic architecure
- Shading needed to see details



Mandelbulb Equation

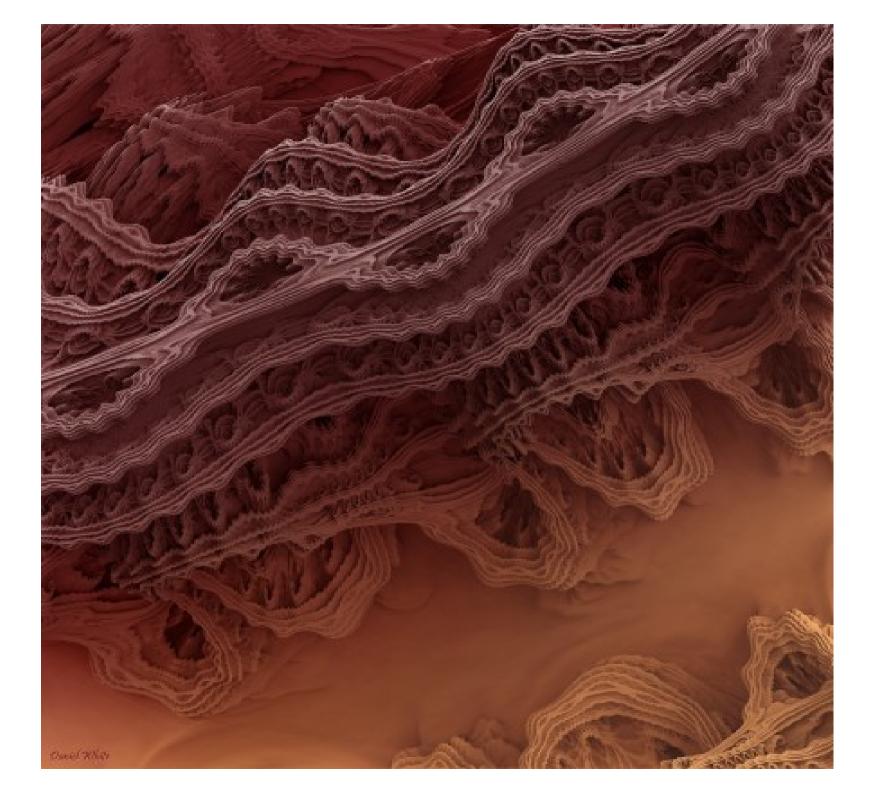
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$$Z_{n+1} = Z_n^2 + C$$

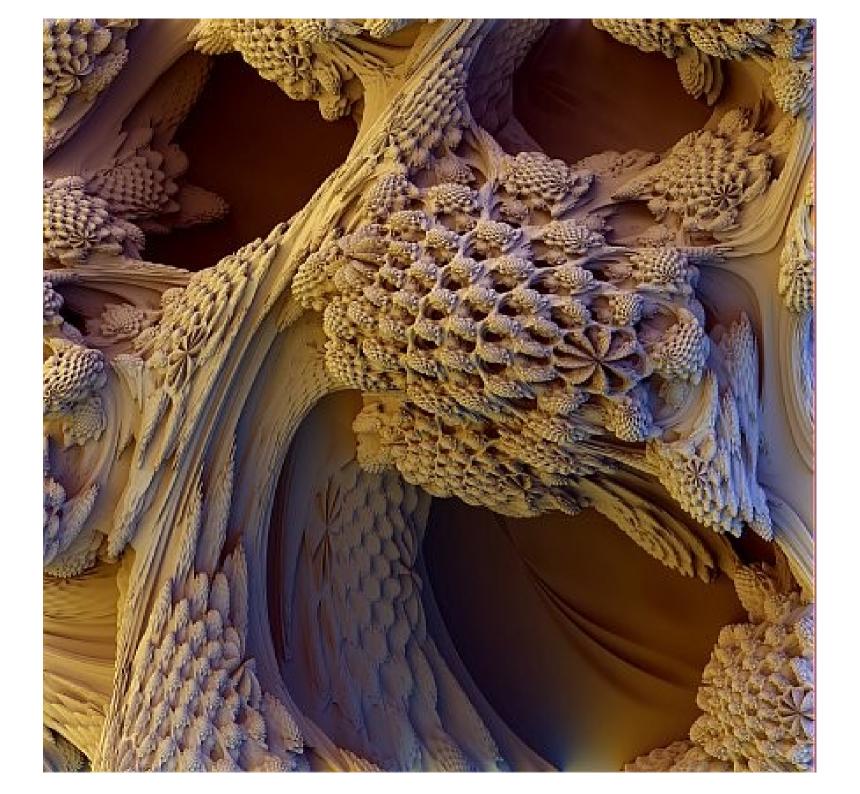
- Domain for this equation converges
- No direct equivalent to complex for 2D
- White and Nylander spherical coordinates
- How do you render this set?
 - POVray used for many images
 - ex26 and ex27 are primitive but real time
- See handout for details

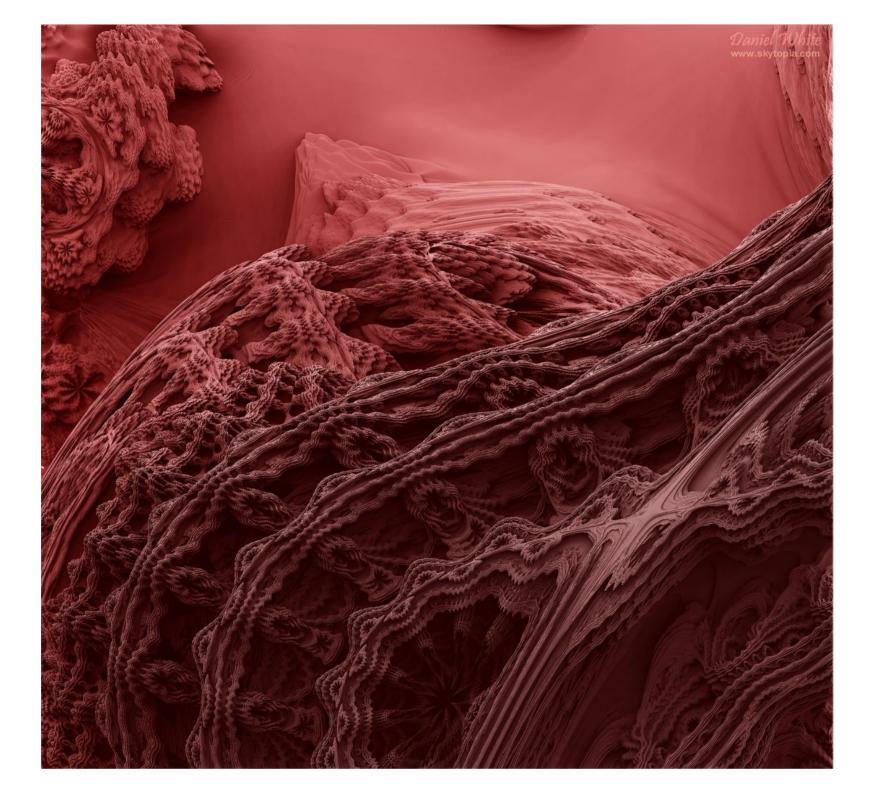
Gallery of Daniel White

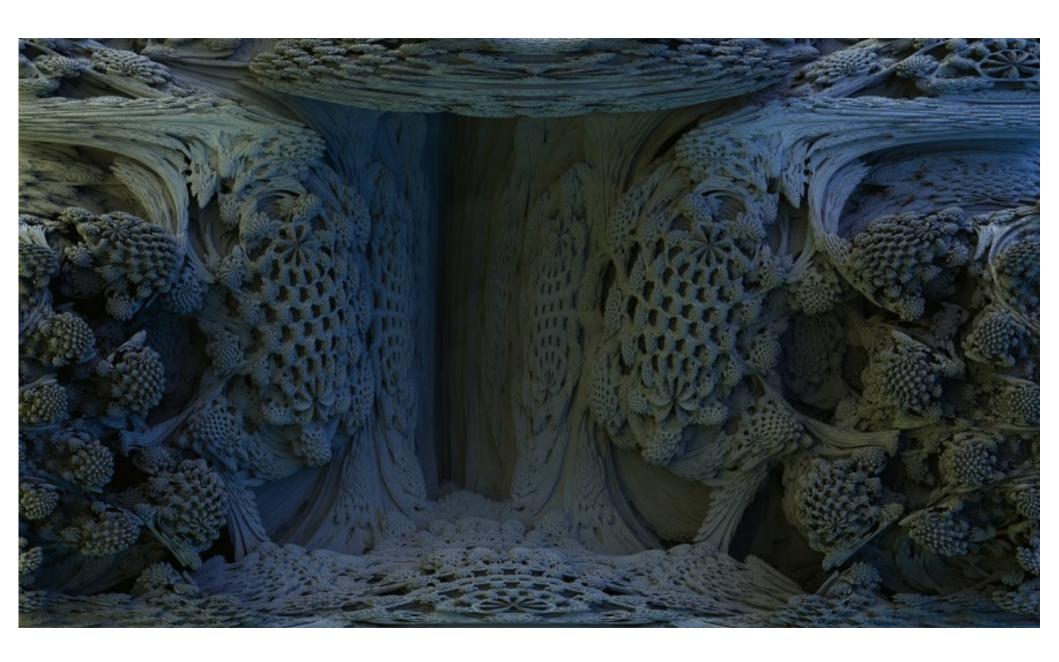
- The Unravelling the Real 3D Mandelbulb http://www.skytopia.com/project/fractal/mandelbulb.html
- Explores and zooms into the mandelbulb
- Ray traced using colored lights
- Most are the n=8 mandelbulb

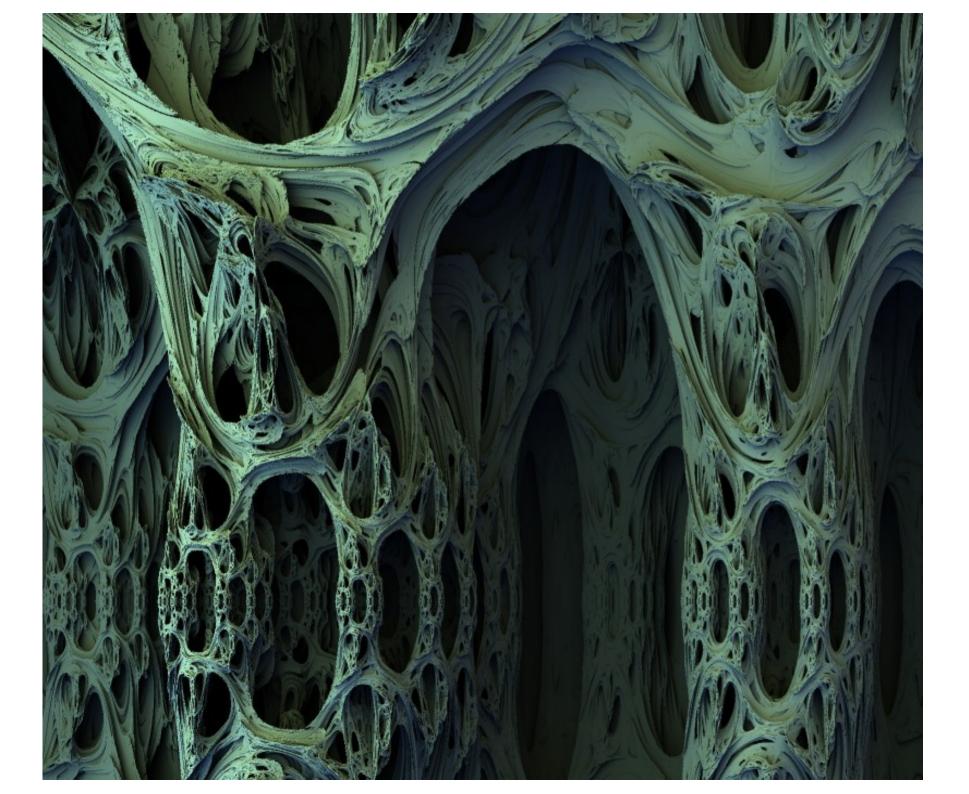


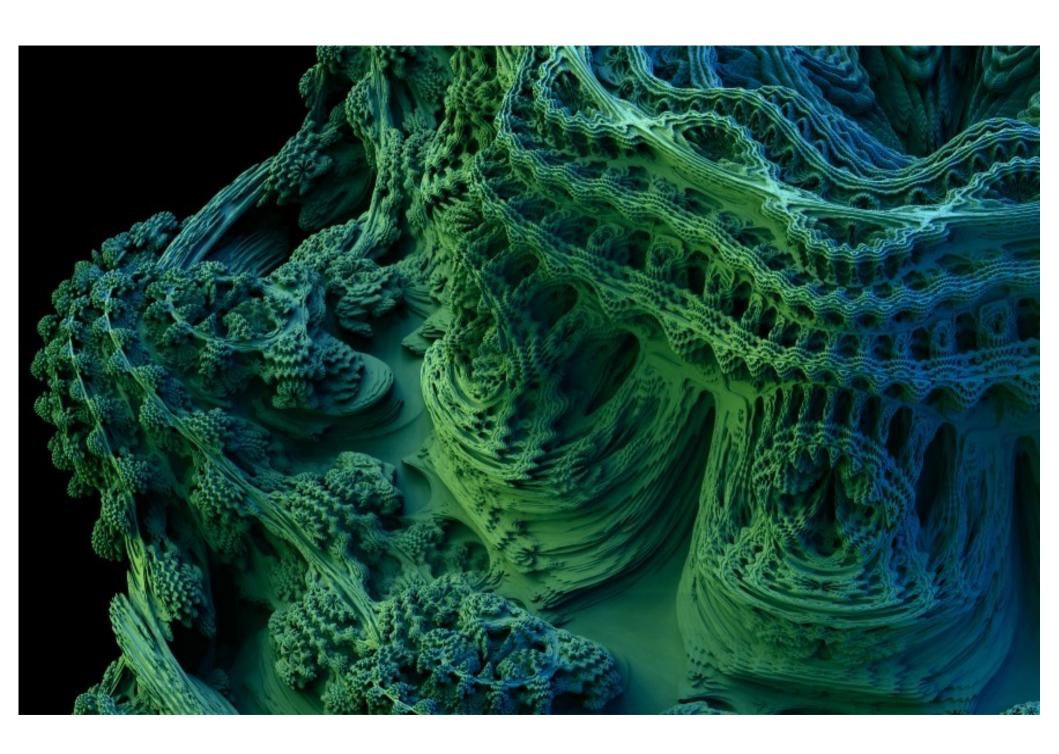






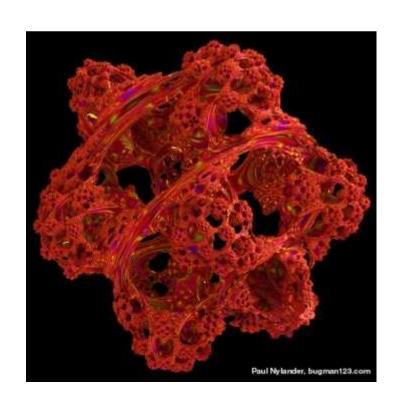






Other Fractal Sets

- Mandelbrot set is just one of many 2D fractal sets
 - Julia
 - Lyapunov
 - Sierpinski triangle
- Many extensions to 3D



Real Time Ray Tracer

- ex26
 - Iterative solver for ray marching
 - OpenMP for parallel rays
- ex27
 - Adapts ex26 to CUDA
- Why not use GLSL?