## **Shadows** CSCI 4229/5229 Computer Graphics Summer 2009

# Shadows in Computer Graphics

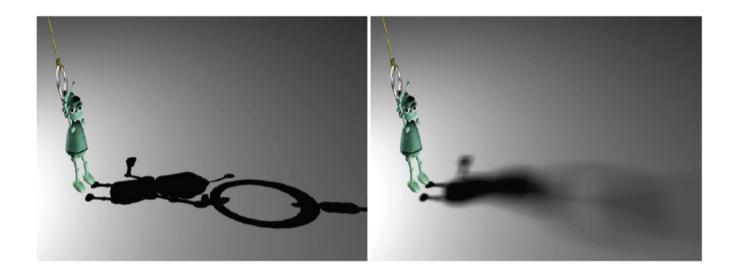
- Shadows are important to realism
  - Depth cues
  - Relative positions of objects
- Doesn't just happen when lighting is turned on
  - Nor is there a glEnable(GL\_SHADOWS)
- Shadows require the scene to be rendered multiple times (at least 2, typically 4)
- Recent (~2000) addition to real time graphics

- Very compute intensive

### **Colorado Fall Colors**



### Soft vs. Hard Shadows

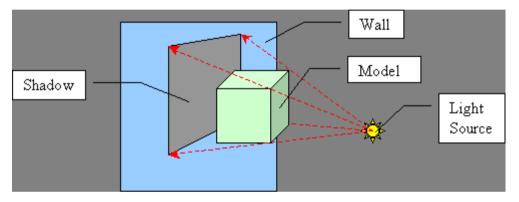


Hard shadow
 *point* light source

- Soft shadow
  *area* light source
- Hard shadows can be done in OpenGL
- Soft shadows not practical in real time
  - Can be approximated by multiple point sources
  - Current research topic

# Planar Shadows

- Projects object on surface
- Simplest shadows
- Fast but very limited
- The problem:



- Surface defined by point E and normal N
- L is the light
- *P* is on the object
- Find *P*' the projection of *P* on the surface

Extend  $\vec{LP}$  to P'

$$P' = L + \lambda(P - L)$$

Let P' be in the plane

$$(P'-E)\cdot N=0$$

Expand P' to

$$(L + \lambda (P - L) - E) \cdot N = 0$$

Then

$$\lambda = \frac{(E-L) \cdot N}{(P-L) \cdot N}$$

so that

$$P' = L + \frac{(E-L) \cdot N}{(P-L) \cdot N} (P-L)$$

Define

$$e = E \cdot N, \quad l = L \cdot N, \quad c = (E - L) \cdot N = e - l$$

Then

$$P' = L + \frac{c}{P \cdot N - l}(P - L)$$

$$P' = L + \frac{c}{P \cdot N - l}(P - L)$$

Expand x component

$$x' = L_x + \frac{cP_x - cL_x}{N_x P_x + N_y P_y + N_z P_z - l}$$
  
=  $\frac{N_x P_x L_x + N_y P_y L_x + N_z P_z L_x - lL_x + cP_x - cL_x}{N_x P_x + N_y P_y + N_z P_z - l}$   
=  $\frac{(N_x L_x + c)P_x + (N_y L_x)P_y + (N_z L_x)P_z - eL_x}{N_x P_x + N_y P_y + N_z P_z - l}$ 

#### Therefore

$$\begin{aligned} x' &= \frac{(N_x L_x + c)P_x + (N_y L_x)P_y + (N_z L_x)P_z - eL_x}{N_x P_x + N_y P_y + N_z P_z - l} \\ y' &= \frac{(N_x L_y)P_x + (N_y L_y + c)P_y + (N_z L_y)P_z - eL_y}{N_x P_x + N_y P_y + N_z P_z - l} \\ z' &= \frac{(N_x L_z)P_x + (N_y L_z)P_y + (N_z L_z + c)P_z - eL_z}{N_x P_x + N_y P_y + N_z P_z - l} \end{aligned}$$

so that

$$\begin{bmatrix} x'\\y'\\z'\\w' \end{bmatrix} = \begin{bmatrix} L_x N_x + c & L_x N_y & L_x N_z & -eL_x\\L_y N_x & L_y N_y + c & L_y N_z & -eL_y\\L_z N_x & L_z N_y & L_z N_z + c & -eL_z\\N_x & N_y & N_z & -l \end{bmatrix} \begin{bmatrix} x\\y\\z\\1 \end{bmatrix}$$